

$$\text{Tooth length} - (\text{verge sep} - \frac{1}{\sqrt{2}} \text{ pallet}) = \text{overlap}$$

$$\text{Tooth} + \frac{1}{\sqrt{2}} \text{ pallet} - \text{verge sep} = \text{overlap}$$

$$1 + \frac{1}{\sqrt{2}T} P - \frac{V}{T} = E$$

$$1 + \frac{1}{\sqrt{2}T} P - \frac{V}{T} \geq 0$$

$$\frac{P}{\sqrt{2}T} \geq \frac{V}{T} - 1$$

$$P \geq \sqrt{2}(V - T)$$

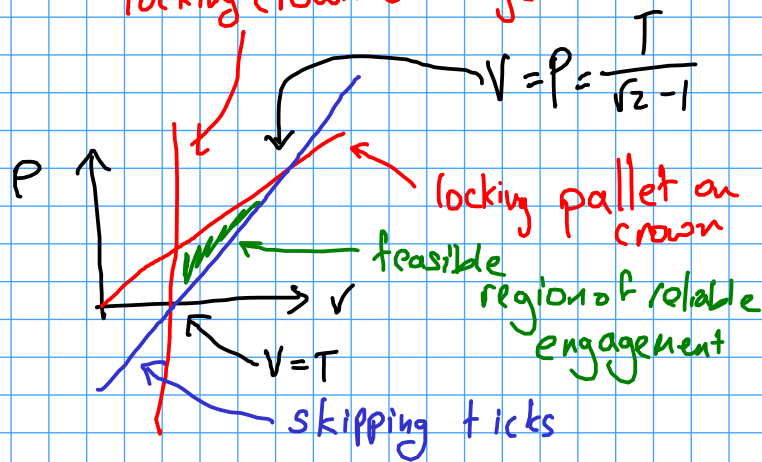
locking pallet on crown

$$V = \sqrt{2}(V - T)$$

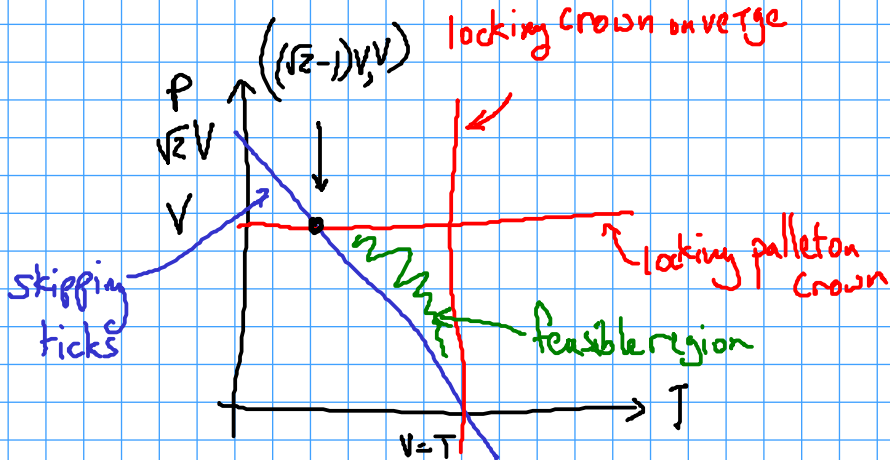
$$(\sqrt{2} - 1)V = T$$

$$V = \frac{1}{\sqrt{2} - 1} T$$

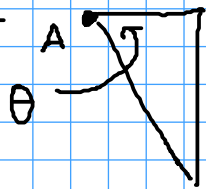
locking crown on verge



locking crown on verge



Finding optimum pallet and tooth length as incenter of feasible region



$$\theta = \text{atan} \frac{-V}{V - (\sqrt{2} - 1)V} = \text{atan} \left(\frac{-1}{\sqrt{2}} \right)$$

equation of angle bisector of A

$$P - V = \tan \left(\frac{1}{2} \text{atan} \frac{-1}{\sqrt{2}} \right) (T - (\sqrt{2} - 1)V)$$

Evaluating when $P = T$:

$$T - V = \tan \left(\frac{1}{2} \text{atan} \frac{-1}{\sqrt{2}} \right) (T - (\sqrt{2} - 1)V)$$

$$= \tan \left(\frac{1}{2} \text{atan} \frac{-1}{\sqrt{2}} \right) T - \tan \left(\frac{1}{2} \text{atan} \frac{-1}{\sqrt{2}} \right) (\sqrt{2} - 1)V$$

$$(1 - \tan \left(\frac{1}{2} \text{atan} \frac{-1}{\sqrt{2}} \right)) T = (1 - \tan \left(\frac{1}{2} \text{atan} \frac{-1}{\sqrt{2}} \right) (\sqrt{2} - 1)) V$$

$$P = T = \frac{(1 - \tan \left(\frac{1}{2} \text{atan} \frac{-1}{\sqrt{2}} \right) (\sqrt{2} - 1)) V}{(1 - \tan \left(\frac{1}{2} \text{atan} \frac{-1}{\sqrt{2}} \right))}$$

$$\approx 0.86V$$

Minimum length for engaging if $P = T$:

$$P \geq \sqrt{2}(V - T)$$

$$(1 + \sqrt{2})T \geq \sqrt{2}V$$

$$T \geq \frac{\sqrt{2}}{1 + \sqrt{2}} V \approx 0.58V$$